

$$a \in G$$

$$\text{ord } a \mid |G|$$

if $|G|$ is a prime number,

$$\text{ord } a \in \{1, |G|\}$$

$$\text{the } \text{ord } a = 1 \Rightarrow a = \Theta$$

$$\underbrace{a + a + \dots + a = \Theta}$$

$\text{ord } a$ - minimal number of occurrences of a here

$$\text{So if } a \neq \Theta \Rightarrow \text{ord } a = |G|$$

$$\langle a \rangle = G \quad \ddot{\smile}$$

So how to generate an instance for the ~~task~~ L2?

use the sage script: $\mathbb{P}, E_{a,b}(\mathbb{F}_p), \mathbb{P}$

$$\mathbb{P} = (x, y, 1) \rightarrow (x, y)$$

projective coordinate affine

$$\text{ord } P = \#E_{a,b}(\mathbb{F}_p)$$

is prime

let us call it q

Let s be a random element of

$$\{2, 3, \dots, q-1\}$$

and generate:

$$Y = s \cdot P$$

$$\text{Pollard-}\rho(Y, \mathbb{P}, q, p, a, b)$$

basepoint

necessary to define the arithmetic

s'

$$\text{if } s' = s \pmod{q} ?$$

$$Y = s' \cdot P$$

alternatively

Pollard- ρ : we search for a collision between $T = H$?

Can we take advantage of the fact that T and $-T$ (~~the same~~) have the same x coordinate?